

The three digits of a three-digit number add up to 25. How many such three-digit numbers are there?



NumberSense

Mathematics Programme

Breezy

I multiplied two consecutive numbers (e.g. 4 and 5) on my calculator and got the answer 702.
What is the sum of the two numbers?



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Mathematics Programme

Breezy

Split the number 18 into two whole numbers (e.g. 3 and 15). Now multiply these two numbers. What is the largest possible answer?



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Breezy

20 can be written as the sum of two squares,
e.g. $20 = 4 + 16 = 2^2 + 4^2$

In how many different ways (ignore the order)
can 85 be written as the sum of two squares?



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Mathematics Programme

Breezy

How many two-digit numbers are there with both digits even?

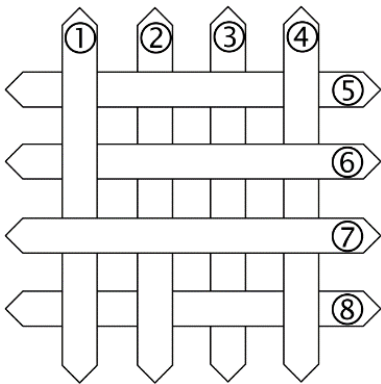


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Breezy

The sketch shows eight lolly sticks. If you must pick up the top one each time, in what order will you pick them up?





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Breezy

What is the smallest ten-digit number that has exactly two digits that are the same and all other digits are different? Note: Numbers cannot start with zero!



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Breezy

The digits of the year 2020 add up to 4. In how many other years (starting from 1), before 2020, has this happened?



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Breezy

There are 60 learners in a class. Always two students share a desk. Every boy shares a desk with a girl. Exactly half the girls share a desk with a boy. How many boys are in the class?



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Breezy

Terri's birthday is on 3 December. On 1 August 2012 she was 11-years-old. In which year will she have her 21st birthday?



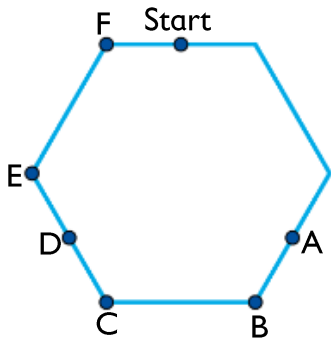
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Breezy

A running track is in the shape of a hexagon with equal sides. Kerri started running from the start flag. She ran an anti-clockwise direction (that is towards F) and stopped one-third of the way around the track.

At which point (A, B, C, D or E) did she stop?





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Breezy

The inter-school soccer league consists of 8 teams. How many matches will each team play if every team plays against every other team twice – once at home and once away?



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Breezy

Mr Safe has a 4-digit combination that opens his lock. He remembers that the four digits are 3, 5, 7 and 9, but he has forgotten the correct order. What is the most different combinations that he must try to open the safe?



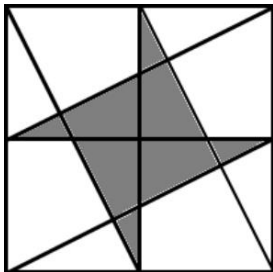
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Breezy

In the diagram, a corner of the shaded star touches the middle of each side of the large square.

What fraction of the large square is NOT shaded?





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So-So

Today is a Monday. Thabo starts to read a book with 290 pages today. On Mondays he reads 25 pages and on every other day he reads 4 pages. On which day of the week does he finish reading the book?



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So-So

There are 14 people at a party. Every pair of people shakes hands exactly once. How many handshakes occur?



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So-So

A painter takes two days to paint a room (all four walls and the ceiling). If he works at the same pace, how many days will he take to paint a room that is twice as wide, twice as long and twice as high?



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So-So

Check this number pattern:

$$1 = 1 \times 1$$

$$1 + 3 = 2 \times 2$$

$$1 + 3 + 5 = 3 \times 3$$

$$1 + 3 + 5 + 7 = 4 \times 4$$

Now calculate $1 + 3 + 5 + 7 + \dots$ all the way up to
 $\dots + 97 + 99$



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So-So

What is the difference between the sum of the even numbers and the sum of the odd numbers from 1 to 100, both included?



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So-So

What is the 83rd number in the following pattern: 1 ; 3 ; 5 ; 7 ;?



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So-So

Consider the following pattern:

$$1^3 + 2^3 = 3^2$$

$$1^3 + 2^3 + 3^3 = 6^2$$

$$1^3 + 2^3 + 3^3 + 4^3 = 10^2$$

$$1^3 + 2^3 + 3^3 + 4^3 + \dots + 10^3 = n^2$$

What is the value of n ?



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So-So

The Olympic committee printed numbered bibs for each of the athletes competing in the ski jump event, starting from the number 1. If 234 digits were printed overall, how many athletes competed?



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So-So

The product of two positive integers is equal to twice their sum. The same product is also equal to six times the difference between the two integers. What is the sum of the integers?



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So-So

What is the value of a in the table?

1	2	3	4	...	a
4	6	8	10	...	64



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So-So

Which one of the following numbers will appear in the sequence: 2; 5; 10; 17; 26; 37; ...?

(A) 901

(B) 902

(C) 903

(D) 904

(E) None of these



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So-So

A series of 10 books were published at 2-year intervals. The sum of the publication years is 20 000. When was the first book published?



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So-So

How many of the 5-digit numbers which consist of the five digits 1, 2, 3, 4 and 5 are divisible by all of 1, 2, 3, 4 and 5?



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So-So

Arnie, Bender and Cross are three robots. They are weighed two at a time. Here are the results:

- $A + B = 12$ kg
- $B + C = 14$ kg
- $C + A = 16$ kg

How much will all three weigh together?



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So-So

Calculate:

$$\frac{1 + 3 + 5 + 7 + \dots + 97 + 99}{2 + 4 + 6 + 8 + \dots + 98 + 100}$$



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Fiendish

Xolile has a bag of marbles. He gave $\frac{1}{3}$ of them to Baba and then $\frac{1}{4}$ of the remaining marbles to Sam. If there are now 24 marbles in the bag, how many marbles did Xolile give to Baba?



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Mathematics Programme

Fiendish

Numbers are arranged in the following patterns:

1	2	3	4	5	6	row 1
7	8	9	10	11	12	row 2
13	14	15	16	17	18	row 3
...	row 4

What will the third number in row 81 be?



NumberSense

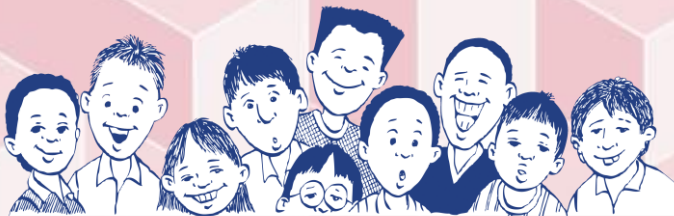
Mathematics Programme

Fiendish

All the counting numbers are arranged in columns as shown below.

A	B	C	D	E	F	G
1	2	3	4	5	6	7
8	9	10	11	12	13	14
15	16	17	18	19	20	21
...

In which column is 500?



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Mathematics Programme

Fiendish

a , b , c and d are four adjacent dates in a calendar as shown.

Mon	Tue	Wed	Thu	Fri	Sat	Sun
		a	b			
		c	d			

Which statement is true for **any** calendar?

- (A) $a + c = b + d$
(C) $c - b = a - d$
(E) $d - a = c + b$

- (B) $a + d = b + c$
(D) $a + b = c + d$



NumberSense

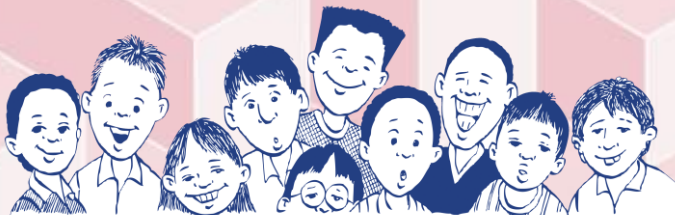
Mathematics Programme

Fiendish

a , b , c and d are four adjacent dates in a calendar as shown.

Mon	Tue	Wed	Thu	Fri	Sat	Sun
		a	b			
		c	d			

What is the value of a if $a + b + c + d = 52$?



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Mathematics Programme

Fiendish

30 students wrote a mathematics exam out of 100 marks. The average score was 50. The average score of those who passed was 60 and the average score of those who failed was 45. How many students passed?

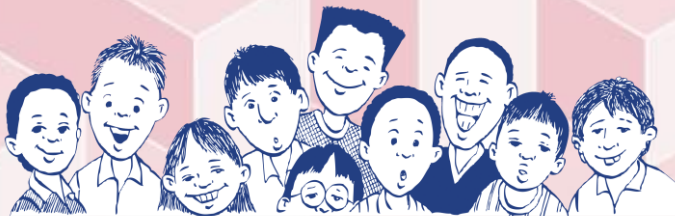


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Mathematics Programme

Fiendish

The average of eleven numbers is 8. If a twelfth number is added to these numbers, the average of all twelve numbers is now 11. What is the twelfth number?

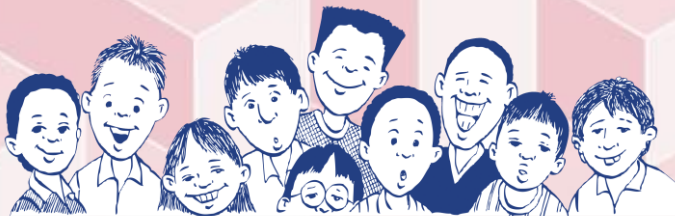


NumberSense

Mathematics Programme

Fiendish

A bath fills in 12 minutes if the plug is in. It empties in 18 minutes when the tap is off. If the tap is running and the plug is out, how long will it take to fill the bath?

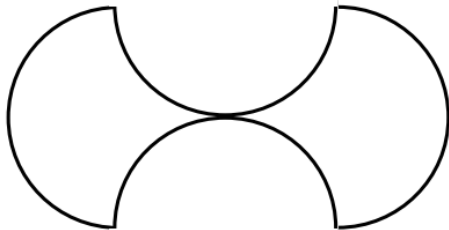


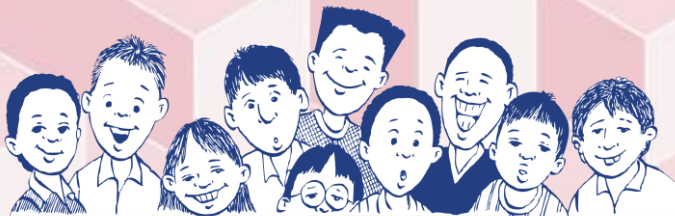
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Mathematics Programme

Fiendish

The figure is a combination of four semi-circles, each with a radius of 3 cm. What is the area of the figure?





NumberSense

Mathematics Programme

Fiendish

A water tank is $\frac{7}{8}$ full. After 420 litres had been drawn from it, it is half full. How many litres does the tank hold when it is full?

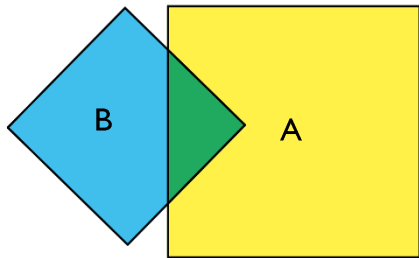


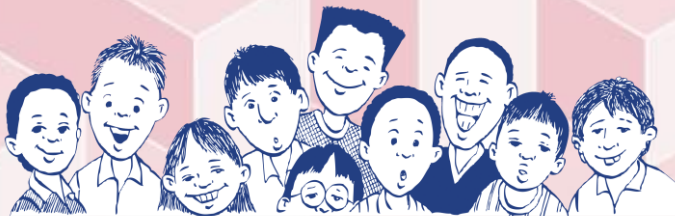
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Fiendish

Two squares with lengths 4 cm and 6 cm respectively, partially overlap as shown in the diagram. What is the difference between shaded area A and shaded area B?





NumberSense

Mathematics Programme

Fiendish